

4762
2006

Mark Scheme

January

Q 1		mark		Sub
(i)	$16 = 0.4v$ so 40 m s^{-1}	M1 A1	Use of $I = \Delta mv$	2
(ii)	PCLM \uparrow +ve $0.4 \times 32 - 0.6u = 0.4v_p + 0.6 \times 4$ NEL \uparrow +ve $\frac{4 - v_p}{-u - 32} = -0.1$ Solving $u = 18$ $v_p = -1$ so 1 m s^{-1} downwards	M1 A1 M1 A1 E1 A1 A1	Use of PCLM Any form Use of NEL. Allow sign errors. Any form Must be obtained from a pair of correct equations. If given $u = 18$ used then $v_p = -1$ must be obtained from 1 equation and both values tested in the second equation cao. Accept use of given $u = 18$ cao	7
(iii)	Considering the momenta involved $0.5 \begin{pmatrix} -3.6 \\ 5.2 \end{pmatrix} = 0.2 \begin{pmatrix} 3 \\ 4 \end{pmatrix} + 0.3 \mathbf{v}_D$ $\mathbf{v}_D = \begin{pmatrix} -8 \\ 6 \end{pmatrix}$ so $a = -8$ and $b = 6$ Gradients of the lines are $\frac{4}{3}$ and $\frac{6}{-8}$ Since $\frac{4}{3} \times \frac{6}{-8} = -1$, they are at 90°	M1 B1 B1 A1 A1 A1 M1 E1	PCLM applied. May be implied. LHS momentum of C correct Complete equation. Accept sign error. cao cao Any method for the angle Clearly shown	8
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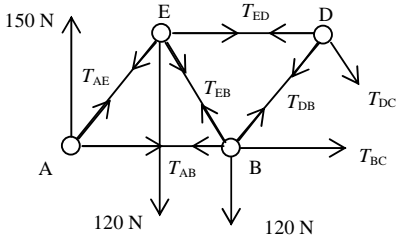
Q		mark		Sub
(i)	<p>Moments about C</p> $240 \times 2 = 3R_D$ $R_D = 160 \text{ so } 160 \text{ N}$ <p>Resolve vertically</p> $R_C + R_D = 240$ $R_C = 80 \text{ so } 80 \text{ N}$	<p>M1</p> <p>A1</p> <p>M1</p> <p>F1</p>	<p>Moments about C or equivalent. Allow 1 force omitted</p> <p>Resolve vertically or moments about D or equivalent.</p> <p>All forces present.</p> <p>FT from their R_D only</p>	4
(ii) (A)	<p>Moments about D</p> $240 \times 1 = 4T \sin 40$ $T = 93.343\dots \text{ so } 93.3 \text{ N (3 s. f.)}$	<p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>Moments about D or equivalent</p> <p>Attempt at resolution for RHS</p> <p>RHS correct</p>	4
(ii) (B)	<p>In equilibrium so horizontal force needed to balance cpt of T. This must be friction and cannot be at C.</p>		<p>Need reference to horizontal force that must come from friction at D.</p>	1
(iii)) (A)	<p>Moments about B</p> $3 \times 240 \times \cos 30 = 6P$ $P = 60\sqrt{3} \text{ (103.92\dots)}$ <p>P inclined at 30° to vertical</p> <p>Resolve horizontally. Friction force F</p> $F = P \sin 30$ $\text{so } F = 30\sqrt{3} \text{ (51.961\dots)}$	<p>M1</p> <p>E1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>All terms present, no extras. Any resolution required attempted.</p> <p>Accept decimal equivalent</p> <p>Seen or equivalent or implied in (iii) (A) or (B).</p> <p>Resolve horizontally. Any resolution required attempted</p> <p>Any form</p>	5

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(iii)) (B)	Resolve vertically. Normal reaction R $P \cos 30 + R = 240$ Using $F = \mu R$ $\mu = \frac{30\sqrt{3}}{240 - 60\sqrt{3} \times \frac{\sqrt{3}}{2}}$ $= \frac{30\sqrt{3}}{240 - 90} = \frac{\sqrt{3}}{5} = 0.34641 \text{ so } 0.346 \text{ (3 s. f.)}$	M1 A1 M1 A1 A1	Resolve vertically. All terms present and resolution attempted Substitute their expressions for F and R cao. Any form. Accept 2 s. f. or better	5
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Q		mark		Sub
3				
(a)				
(i)	$80 \begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = 48 \begin{pmatrix} 6 \\ 2 \end{pmatrix} + 12 \begin{pmatrix} 1 \\ -3 \end{pmatrix} + 20 \begin{pmatrix} 11 \\ 9 \end{pmatrix}$ $80 \begin{pmatrix} \bar{x} \\ \bar{y} \end{pmatrix} = \begin{pmatrix} 520 \\ 240 \end{pmatrix}$ $\bar{x} = 6.5$ $\bar{y} = 3$	M1 B1 B1 E1 A1	Correct method for c.m. Total mass correct One c.m. on RHS correct [If separate components considered, B1 for 2 correct] cao	5
(ii)	Consider x coordinate $520 = 76 \times 6.4 + 4x$ so $x = 8.4$	M1 B1 A1	Using additive principle o. e. on x cpts Areas correct. Allow FT from masses from (i) cao	3
(iii)	y coordinate is 1 so we need $240 = 76\bar{y} + 4 \times 1$ and $\bar{y} = 3.10526\dots$ so 3.11 (3 s. f.)	B1 M1 A1	Position of centre of square cao	3
(b)				
(i)	Moments about C $4R = 120 \times 3 + 120 \times 2$ so $4R = 600$ and $R = 150$	M1 E1	Moments equation. All terms present	2
(ii)	 $A \uparrow 150 + T_{AE} \cos 30 = 0$ $T_{AE} = -100\sqrt{3}$ so $100\sqrt{3}$ N (C) $E \downarrow 120 + T_{AE} \cos 30 + T_{EB} \cos 30 = 0$ $T_{EB} = 20\sqrt{3}$ so $20\sqrt{3}$ N (T)	B1 M1 A1 M1 F1 F1	Equilibrium at a pin-joint Any form. Sign correct. Neglect (C) Equilibrium at E, all terms present Any form. Sign follows working. Neglect (T). T/C consistent with answers	

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(iii)	Consider \rightarrow at E, using (ii) gives ED as thrust	E1	Clearly explained. Accept 'thrust' correctly deduced from wrong answers to (ii).	1
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Q		mark		Sub
4				
(i)	$\frac{0.5 \times 20 \times 8^2 - 0.5 \times 20 \times 5^2 + 510}{6}$ = 150 W	M1 B1 A1 A1	Use of $P = WD/t$ ΔKE . Accept ± 390 soi All correct including signs	4
(ii) (A)	$20g \times \frac{3}{5}x - 5gx$ $7gx$ (68.6x) gain	M1 B1 A1 A1	Use of mgh on both terms Either term (neglecting signs) $\pm 7gx$ in any form. cao	4
(B)	11gx	B1		1
(C)	$0.5 \times 25 \times 4^2 = 7gx + 11gx = 18gx$ $x = 1.13378\dots$ so 1.13 m (3 s. f.)	M1 B1 A1	Use of work-energy equation. Allow 1 RHS term omitted. KE term correct cao. Except follow wrong sign for $7gx$ only.	3
(iii))	either $0.5 \times 35 \times v^2 - 0.5 \times 35 \times 16$ $= 15g \times 0.5 - 11g \times 0.5 - 12g \times 0.5$ $v^2 = 13.76$ so $v = 3.70944\dots$ so 3.71 m s^{-1} (3 s. f.) or $15g - T = 15a \quad T - 12g - 11g = 20a$ so $a = -2.24$ $v^2 = 4^2 + 2 \times (-2.24) \times 0.5$ so 3.71 m s^{-1} (3 s. f.)	M1 B1 A1 A1 M1 A1 M1 A1	Use of work-energy. KE, GPE and WD against friction terms present. ΔGPE correct inc sign (1.5g J loss) All correct cao N2L in 1 or 2 equations. All terms present cao Use of appropriate (sequence of) $uvast$ cao	4
				16